Package 'MKpower'

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Description Power analysis and sample size calculation for Welch and Hsu (Hedderich and Sachs (2018), ISBN:978-3-662-56657-2) t-tests including Monte-Carlo simulations of empirical power and type-I-error. Power and sample size calculation for Wilcoxon rank sum and signed rank tests via Monte-Carlo simulations. Power and sample size required for the evaluation of a diagnostic test(-system) (Flahault et al. (2005), <doi:10.1016/j.jclinepi.2004.12.009>; Dobbin and Simon (2007), <doi:10.1093/biostatistics/kxj036>) as well as for a single proportion (Fleiss et al. (2003), ISBN:978-0-471-52629-2; Piegorsch (2004), <doi:10.1016/j.csda.2003.10.002>; Thulin (2014), <doi:10.1214/14-ejs909>), comparing two negative binomial rates (Zhu and Lakkis (2014), <doi:10.1002/sim.5947>), ANCOVA (Shieh (2020), <doi:10.1007/s11336-019-09692-3>), reference ranges (Jennen-Steinmetz and Wellek (2005), <doi:10.1002/sim.2177>), and multiple primary endpoints (Sozu et al. (2015), ISBN:978-3-319-22005-5).

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`MKpower-package` *Power Analysis and Sample Size Calculation.*

Description

Power analysis and sample size calculation for Welch and Hsu (Hedderich and Sachs (2018), ISBN:978-3-662-56657-2) t-tests including Monte-Carlo simulations of empirical power and type-I-error. Power and sample size calculation for Wilcoxon rank sum and signed rank tests via Monte-Carlo simulations. Power and sample size required for the evaluation of a diagnostic test(-system) (Flahault et al. (2005), <doi:10.1016/j.jclinepi.2004.12.009>; Dobbin and Simon (2007), <doi:10.1093/biostatistics/kxj036>) as well as for a single proportion (Fleiss et al. (2003), ISBN:978-0-471-52629-2; Piegorsch (2004), <doi:10.1016/j.csda.2003.10.002>; Thulin (2014), <doi:10.1214/14-ejs909>), comparing two negative binomial rates (Zhu and Lakkis (2014), <doi:10.1002/sim.5947>), ANCOVA (Shieh (2020), <doi:10.1007/s11336-019-09692-3>), reference ranges (Jennen-Steinmetz and Wellek (2005), <doi:10.1002/sim.2177>), and multiple primary endpoints (Sozu et al. (2015), ISBN:978-3-319-22005-5).

Details

library(MKpower)

Author(s)

Matthias Kohl https://www.stamats.de

Maintainer: Matthias Kohl <matthias.kohl@stamats.de>

`hist` *Histograms*

Description

Produce histograms for simulations of power and type-I-error of tests.

Usage

```
## S3 method for class 'sim.power.ttest'
hist(x, color.hline = "orange", ...)

## S3 method for class 'sim.power.wtest'
hist(x, color.hline = "orange", ...)
```

Arguments

`x`	object of class `sim.power.ttest`.
`color.hline`	color of horizontal line indicating uniform distribution of p values.
`...`	further arguments that may be passed through).

Details

The plot generates a `ggplot2` object that is shown.

Missing values are handled by the `ggplot2` functions.

Value

Object of class gg and `ggplot`.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

See Also

`hist`

Examples

```
res1 <- sim.power.t.test(nx = 5, rx = rnorm, rx.H0 = rnorm,
                         ny = 10, ry = function(x) rnorm(x, mean = 3, sd = 3),
                         ry.H0 = function(x) rnorm(x, sd = 3))
hist(res1)
res2 <- sim.power.wilcox.test(nx = 6, rx = rnorm, rx.H0 = rnorm,
                       ny = 6, ry = function(x) rnorm(x, mean = 2),
                       ry.H0 = rnorm)
hist(res2)
```

---

power.ancova *Power Calculation for ANCOVA*

Description

Compute sample size for ANCOVA.

Usage

```
power.ancova(n = NULL, mu = NULL, var = 1, nr.covs = 1L, group.ratio = NULL,
             contr.mat = NULL, sig.level = 0.05, power = NULL, n.max = 1000L,
             rel.tol = .Machine$double.eps^0.25)
```

Arguments

n	vector of sample sizes per groups.
mu	vector of mean values of the groups.
var	error variance.
nr.covs	number of covariates (larger or equal than 1).
group.ratio	vector of group sizes relative to group 1; i.e., first entry should always be one. If NULL, a balanced design is used.
contr.mat	matrix of contrasts (number of columns must be idential to number of groups). If NULL, standard ANCOVA contrasts are used; see examples below.
sig.level	significance level (type I error probability)
power	power of test (1 minus type II error probability)
n.max	maximum sample size considered in the computations.
rel.tol	relative tolerance passed to function integrate.

Details

Exactly one of the parameters n and power must be passed as NULL, and that parameter is determined from the other.

The function includes an implementation of the exact approach of Shieh (2020). It is based on the code provided in the supplement of Shieh (2020), but uses integrate instead of the trapezoid rule and uniroot for finding the required sample size.

Value

Object of class "power.htest", a list of the arguments (including the computed one) augmented with a note element.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

G. Shieh (2020). Power Analysis and Sample Size Planning in ANCOVA Designs. *Psychometrika* **85**:101-120. doi:10.1007/s11336019096923.

S.E. Maxwell and H.D. Delaney (2004). *Designing experiments and analyzing data: A model comparison perspective* (2nd ed.). Mahwah, NJ: Lawrence Erlbaum Associates.

See Also

power.anova.test, power.t.test

Examples

```
## Default matrix of contrasts
## 3 groups
cbind(rep(1,2), -diag(2))
## 4 groups
cbind(rep(1,3), -diag(3))

## Table 1 in Shieh (2020)
power.ancova(mu=c(400, 450, 500), var = 9900, power = 0.8)
power.ancova(n = rep(63/3, 3), mu=c(400, 450, 500), var = 9900)
power.ancova(mu=c(400, 450, 500), var = 9900, power = 0.8, nr.covs = 10)
power.ancova(n = rep(72/3, 3), mu=c(400, 450, 500), var = 9900, nr.covs = 10)

## Table 2 in Shieh (2020)
power.ancova(mu=c(400, 450, 500), var = 7500, power = 0.8)
power.ancova(n = rep(48/3, 3), mu=c(400, 450, 500), var = 7500)
power.ancova(mu=c(400, 450, 500), var = 7500, power = 0.8, nr.covs = 10)
power.ancova(n = rep(60/3, 3), mu=c(400, 450, 500), var = 7500, nr.covs = 10)

## Table 3 in Shieh (2020)
power.ancova(mu=c(400, 450, 500), var = 1900, power = 0.8)
power.ancova(n = rep(18/3, 3), mu=c(400, 450, 500), var = 1900)
power.ancova(mu=c(400, 450, 500), var = 1900, power = 0.8, nr.covs = 10)
power.ancova(n = rep(27/3, 3), mu=c(400, 450, 500), var = 1900, nr.covs = 10)

## ANOVA approach for Table 1-3
power.anova.test(groups = 3, between.var = var(c(400, 450, 500)),
                 within.var = 10000, power = 0.8)
power.anova.test(n = 63/3, groups = 3, between.var = var(c(400, 450, 500)),
                 within.var = 10000)
```

```
## Table 4 in Shieh (2020)
power.ancova(mu=c(410, 450, 490), var = 9900, power = 0.8)
power.ancova(n = rep(96/3, 3), mu=c(410, 450, 490), var = 9900)
power.ancova(mu=c(410, 450, 490), var = 9900, power = 0.8, nr.covs = 10)
power.ancova(n = rep(105/3, 3), mu=c(410, 450, 490), var = 9900, nr.covs = 10)

## Table 5 in Shieh (2020)
power.ancova(mu=c(410, 450, 490), var = 7500, power = 0.8)
power.ancova(n = rep(72/3, 3), mu=c(410, 450, 490), var = 7500)
power.ancova(mu=c(410, 450, 490), var = 7500, power = 0.8, nr.covs = 10)
power.ancova(n = rep(84/3, 3), mu=c(410, 450, 490), var = 7500, nr.covs = 10)

## Table 6 in Shieh (2020)
power.ancova(mu=c(410, 450, 490), var = 1900, power = 0.8)
power.ancova(n = rep(24/3, 3), mu=c(410, 450, 490), var = 1900)
power.ancova(mu=c(410, 450, 490), var = 1900, power = 0.8, nr.covs = 10)
power.ancova(n = rep(33/3, 3), mu=c(410, 450, 490), var = 1900, nr.covs = 10)

## ANOVA approach for Table 4-6
power.anova.test(groups = 3, between.var = var(c(410, 450, 490)),
                 within.var = 10000, power = 0.8)
power.anova.test(n = 96/3, groups = 3, between.var = var(c(410, 450, 490)),
                 within.var = 10000)

################################################################################
## Example from Maxwell and Delaney (2004) according to Shieh (2020)
################################################################################
## ANCOVA (balanced design)
power.ancova(n = rep(30/3, 3), mu=c(7.5366, 11.9849, 13.9785), var = 29.0898)
power.ancova(mu=c(7.5366, 11.9849, 13.9785), var = 29.0898, power = 0.8)
power.ancova(mu=c(7.5366, 11.9849, 13.9785), var = 29.0898, power = 0.9)

## ANOVA
power.anova.test(n = 30/3, groups = 3, between.var = var(c(7.5366, 11.9849, 13.9785)),
                 within.var = 29.0898)
power.anova.test(groups = 3, between.var = var(c(7.5366, 11.9849, 13.9785)),
                 within.var = 29.0898, power = 0.8)
power.anova.test(groups = 3, between.var = var(c(7.5366, 11.9849, 13.9785)),
                 within.var = 29.0898, power = 0.9)

## ANCOVA - imbalanced design
power.ancova(mu=c(7.5366, 11.9849, 13.9785), var = 29.0898, power = 0.8,
             group.ratio = c(1, 1.25, 1.5))
power.ancova(n = c(13, 16, 19), mu=c(7.5366, 11.9849, 13.9785), var = 29.0898,
             group.ratio = c(1, 1.25, 1.5))
power.ancova(mu=c(7.5366, 11.9849, 13.9785), var = 29.0898, power = 0.8,
             group.ratio = c(1, 0.8, 2/3))
power.ancova(n = c(17, 14, 12), mu=c(7.5366, 11.9849, 13.9785), var = 29.0898,
             group.ratio = c(1, 0.8, 2/3))
```

---

power.diagnostic.test *Power Calculations for Diagnostic Tests*

Description

Compute sample size, power, delta, or significance level of a diagnostic test for an expected sensitivy or specificity.

Usage

```
power.diagnostic.test(sens = NULL, spec = NULL,
                      n = NULL, delta = NULL, sig.level = 0.05,
                      power = NULL, prev = NULL,
                      method = c("exact", "asymptotic"),
                      NMAX = 1e4)
```

Arguments

sens	Expected sensitivity; either sens or spec has to be specified.
spec	Expected specificity; either sens or spec has to be specified.
n	Number of cases if sens and number of controls if spec is given.
delta	sens-delta resp. spec-delta is used as lower confidence limit
sig.level	Significance level (Type I error probability)
power	Power of test (1 minus Type II error probability)
prev	Expected prevalence, if NULL prevalence is ignored which means prev = 0.5 is assumed.
method	exact or asymptotic formula; default "exact".
NMAX	Maximum sample size considered in case method = "exact".

Details

Either sens or spec has to be specified which leads to computations for either cases or controls.

Exactly one of the parameters n, delta, sig.level, and power must be passed as NULL, and that parameter is determined from the others. Notice that sig.level has a non-NULL default so NULL must be explicitly passed if you want to compute it.

The computations are based on the formulas given in the Appendix of Flahault et al. (2005). Please be careful, in Equation (A1) the numerator should be squared, in equation (A2) and (A3) the second exponent should be n-i and not i.

As noted in Chu and Cole (2007) power is not a monotonically increasing function in n but rather saw toothed (see also Chernick and Liu (2002)). Hence, in our calculations we use the more conservative approach II); i.e., the minimum sample size n such that the actual power is larger or equal power andsuch that for any sample size larger than n it also holds that the actual power is larger or equal power.

Value

Object of class "power.htest", a list of the arguments (including the computed one) augmented with method and note elements.

Note

uniroot is used to solve power equation for unknowns, so you may see errors from it, notably about inability to bracket the root when invalid arguments are given.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

A. Flahault, M. Cadilhac, and G. Thomas (2005). Sample size calculation should be performed for design accuracy in diagnostic test studies. *Journal of Clinical Epidemiology*, **58**(8):859-862.

H. Chu and S.R. Cole (2007). Sample size calculation using exact methods in diagnostic test studies. *Journal of Clinical Epidemiology*, **60**(11):1201-1202.

M.R. Chernick amd C.Y. Liu (2002). The saw-toothed behavior of power versus sample size and software solutions: single binomial proportion using exact methods. *Am Stat*, **56**:149-155.

See Also

uniroot

Examples

```
## see n2 on page 1202 of Chu and Cole (2007)
power.diagnostic.test(sens = 0.99, delta = 0.14, power = 0.95) # 40
power.diagnostic.test(sens = 0.99, delta = 0.13, power = 0.95) # 43
power.diagnostic.test(sens = 0.99, delta = 0.12, power = 0.95) # 47

power.diagnostic.test(sens = 0.98, delta = 0.13, power = 0.95) # 50
power.diagnostic.test(sens = 0.98, delta = 0.11, power = 0.95) # 58

## see page 1201 of Chu and Cole (2007)
power.diagnostic.test(sens = 0.95, delta = 0.1, n = 93) ## 0.957
power.diagnostic.test(sens = 0.95, delta = 0.1, n = 93, power = 0.95,
                      sig.level = NULL) ## 0.0496
power.diagnostic.test(sens = 0.95, delta = 0.1, n = 102) ## 0.968
power.diagnostic.test(sens = 0.95, delta = 0.1, n = 102, power = 0.95,
                      sig.level = NULL) ## 0.0471
## yields 102 not 93!
power.diagnostic.test(sens = 0.95, delta = 0.1, power = 0.95)
```

---

power.hsu.t.test *Power Calculations for Two-sample Hsu t Test*

Description

Compute the power of the two-sample Hsu t test, or determine parameters to obtain a target power; see Section 7.4.4 in Hedderich and Sachs (2016).

Usage

```
power.hsu.t.test(n = NULL, delta = NULL, sd1 = 1, sd2 = 1, sig.level = 0.05,
                 power = NULL, alternative = c("two.sided", "one.sided"),
                 strict = FALSE, tol = .Machine$double.eps^0.25)
```

Arguments

n	number of observations (per group)
delta	(expected) true difference in means
sd1	(expected) standard deviation of group 1
sd2	(expected) standard deviation of group 2
sig.level	significance level (Type I error probability)
power	power of test (1 minus Type II error probability)
alternative	one- or two-sided test. Can be abbreviated.
strict	use strict interpretation in two-sided case
tol	numerical tolerance used in root finding, the default providing (at least) four significant digits.

Details

Exactly one of the parameters n, delta, power, sd1, sd2 and sig.level must be passed as NULL, and that parameter is determined from the others. Notice that the last three have non-NULL defaults, so NULL must be explicitly passed if you want to compute them.

If strict = TRUE is used, the power will include the probability of rejection in the opposite direction of the true effect, in the two-sided case. Without this the power will be half the significance level if the true difference is zero.

Value

Object of class "power.htest", a list of the arguments (including the computed one) augmented with method and note elements.

Note

The function and its documentation was adapted from power.t.test implemented by Peter Dalgaard and based on previous work by Claus Ekstroem.

uniroot is used to solve the power equation for unknowns, so you may see errors from it, notably about inability to bracket the root when invalid arguments are given.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

J. Hedderich, L. Sachs. *Angewandte Statistik: Methodensammlung mit R*. Springer 2016.

See Also

power.welch.t.test, power.t.test, t.test, uniroot

Examples

```
## more conservative than classical or Welch t-test
power.hsu.t.test(n = 20, delta = 1)
power.hsu.t.test(power = .90, delta = 1)
power.hsu.t.test(power = .90, delta = 1, alternative = "one.sided")

## sd1 = 0.5, sd2 = 1
power.welch.t.test(delta = 0.5, sd1 = 0.5, sd2 = 1, power = 0.9)
power.hsu.t.test(delta = 0.5, sd1 = 0.5, sd2 = 1, power = 0.9)


if(require(MKinfer)){
## empirical check
M <- 10000
ps <- numeric(M)
for(i in seq_len(M)){
  x <- rnorm(55, mean = 0, sd = 0.5)
  y <- rnorm(55, mean = 0.5, sd = 1.0)
  ps[i] <- hsu.t.test(x, y)$p.value
}
## empirical power
sum(ps < 0.05)/M
}
```

---

power.mpe.atleast.one *Power for at least One Endpoint with Known Covariance*

Description

The function calculates either sample size or power for continuous multiple primary endpoints for at least one endpoint with known covariance.

Usage

```
power.mpe.atleast.one(K, n = NULL, delta = NULL, Sigma, SD, rho, sig.level = 0.05/K,
                      power = NULL, n.max = 1e5, tol = .Machine$double.eps^0.25)
```

Arguments

K	number of endpoints
n	optional: sample size
delta	expected effect size
Sigma	A covariance of known matrix

SD	known standard deviations (length K)
rho	known correlations (length 0.5*K*(K-1))
sig.level	Significance level (Type I error probability)
power	optional: Power of test (1 minus Type II error probability)
n.max	upper end of the interval to be search for n via uniroot.
tol	The desired accuracy

Details

The function can be used to either compute sample size or power for continuous multiple primary endpoints with known covariance where a significant difference for at least one endpoint is expected. The implementation is based on the formulas given in the references below.

The null hypothesis reads $\mu_{Tk} - \mu_{Ck} \leq 0$ for all $k \in \{1, \ldots, K\}$ where Tk is treatment k, Ck is control k and K is the number of co-primary endpoints.

One has to specify either n or power, the other parameter is determined. Moreover, either covariance matrix Sigma or standard deviations SD and correlations rho must be given.

Value

Object of class power.mpe.test, a list of arguments (including the computed one) augmented with method and note elements.

Note

The function first appeared in package **mpe**, which is now archived on CRAN.

Author(s)

Srinath Kolampally, Matthias Kohl <Matthias.Kohl@stamats.de>

References

Sugimoto, T. and Sozu, T. and Hamasaki, T. (2012). A convenient formula for sample size calculations in clinical trials with multiple co-primary continuous endpoints. *Pharmaceut. Statist.*, **11**: 118-128. doi:10.1002/pst.505

Sozu, T. and Sugimoto, T. and Hamasaki, T. and Evans, S.R. (2015). *Sample Size Determination in Clinical Trials with Multiple Endpoints*. Springer Briefs in Statistics, ISBN 978-3-319-22005-5.

Examples

```
## compute power
power.mpe.atleast.one(K = 2, delta = c(0.2,0.2), Sigma = diag(c(1,1)), power = 0.8)

## compute sample size
power.mpe.atleast.one(K = 2, delta = c(0.2,0.2), Sigma = diag(c(2,2)), power = 0.9)

## known covariance matrix
Sigma <- matrix(c(1.440, 0.840, 1.296, 0.840,
```

```
                  0.840, 1.960, 0.168, 1.568,
                  1.296, 0.168, 1.440, 0.420,
                  0.840, 1.568, 0.420, 1.960), ncol = 4)
## compute power
power.mpe.atleast.one(K = 4, n = 60, delta = c(0.5, 0.75, 0.5, 0.75), Sigma = Sigma)
## equivalent: known SDs and correlation rho
power.mpe.atleast.one(K = 4, n = 60, delta = c(0.5, 0.75, 0.5, 0.75),
                      SD = c(1.2, 1.4, 1.2, 1.4),
                      rho = c(0.5, 0.9, 0.5, 0.1, 0.8, 0.25))
```

`power.mpe.known.var` *Multiple Co-Primary Endpoints with Known Covariance*

Description

The function calculates either sample size or power for continuous multiple co-primary endpoints with known covariance.

Usage

```
power.mpe.known.var(K, n = NULL, delta = NULL, Sigma, SD, rho,
  sig.level = 0.05, power = NULL, n.max = 1e5, tol = .Machine$double.eps^0.25)
```

Arguments

`K`	number of co-primary endpoints
`n`	optional: sample size
`delta`	expected effect size (length `K`)
`Sigma`	known covariance matrix (dimension `K` x `K`)
`SD`	known standard deviations (length `K`)
`rho`	known correlations (length `0.5*K*(K-1)`)
`sig.level`	significance level (Type I error probability)
`power`	optional: power of test (1 minus Type II error probability)
`n.max`	upper end of the interval to be search for `n` via `uniroot`.
`tol`	the desired accuracy for `uniroot`.

Details

The function can be used to either compute sample size or power for continuous multiple co-primary endpoints with known covariance where a multivariate normal distribution is assumed. The implementation is based on the formulas given in the references below.

The null hypothesis reads $\mu_{Tk} - \mu_{Ck} \leq 0$ for at least one $k \in \{1, \ldots, K\}$ where Tk is treatment k, Ck is control k and K is the number of co-primary endpoints.

One has to specify either `n` or `power`, the other parameter is determined. Moreover, either covariance matrix `Sigma` or standard deviations `SD` and correlations `rho` must be given.

Value

Object of class `power.mpe.test`, a list of arguments (including the computed one) augemented with method and note elements.

Note

The function first appeared in package **mpe**, which is now archived on CRAN.

Author(s)

Srinath Kolampally, Matthias Kohl <Matthias.Kohl@stamats.de>

References

Sugimoto, T. and Sozu, T. and Hamasaki, T. (2012). A convenient formula for sample size calculations in clinical trials with multiple co-primary continuous endpoints. *Pharmaceut. Statist.*, **11**: 118-128. doi:10.1002/pst.505

Sozu, T. and Sugimoto, T. and Hamasaki, T. and Evans, S.R. (2015). *Sample Size Determination in Clinical Trials with Multiple Endpoints*. Springer Briefs in Statistics, ISBN 978-3-319-22005-5.

See Also

`power.mpe.unknown.var`

Examples

```
## compute power
power.mpe.known.var(K = 2, n = 20, delta = c(1,1), Sigma = diag(c(1,1)))

## compute sample size
power.mpe.known.var(K = 2, delta = c(1,1), Sigma = diag(c(2,2)), power = 0.9,
                    sig.level = 0.025)

## known covariance matrix
Sigma <- matrix(c(1.440, 0.840, 1.296, 0.840,
                  0.840, 1.960, 0.168, 1.568,
                  1.296, 0.168, 1.440, 0.420,
                  0.840, 1.568, 0.420, 1.960), ncol = 4)
## compute power
power.mpe.known.var(K = 4, n = 60, delta = c(0.5, 0.75, 0.5, 0.75), Sigma = Sigma)
## equivalent: known SDs and correlation rho
power.mpe.known.var(K = 4, n = 60,delta = c(0.5, 0.75, 0.5, 0.75),
                    SD = c(1.2, 1.4, 1.2, 1.4),
                    rho = c(0.5, 0.9, 0.5, 0.1, 0.8, 0.25))
```

power.mpe.unknown.var *Multiple Co-Primary Endpoints with Unknown Covariance*

Description

The function calculates either sample size or power for continuous multiple co-primary endpoints with unknown covariance.

Usage

```
power.mpe.unknown.var(K, n = NULL, delta = NULL, Sigma, SD, rho, sig.level = 0.05,
                      power = NULL, M = 10000, n.min = NULL, n.max = NULL,
                      tol = .Machine$double.eps^0.25, use.uniroot = TRUE)
```

Arguments

K	number of co-primary endpoints
n	optional: sample size
delta	expected effect size (length K)
Sigma	unknown covariance matrix (dimension K x K)
SD	unknown standard deviations (length K)
rho	unknown correlations (length 0.5*K*(K-1))
sig.level	significance level (Type I error probability)
power	optional: power of test (1 minus Type II error probability)
M	Number of replications for the required simulations.
n.min	Starting point of search interval for sample size
n.max	End point of search interval for sample size, must be larger than n.min
tol	the desired accuracy for uniroot
use.uniroot	Finds one root of one equation

Details

The function can be used to either compute sample size or power for continuous multiple co-primary endpoints with unknown covariance. The implementation is based on the formulas given in the references below.

The null hypothesis reads $\mu_{Tk} - \mu_{Ck} \leq 0$ for at least one $k \in \{1, \ldots, K\}$ where Tk is treatment k, Ck is control k and K is the number of co-primary endpoints.

One has to specify either n or power, the other parameter is determined. An approach to calculate sample size n, is to first call power.mpe.known.var and use the result as n.min. The input for n.max must be larger then n.min. Moreover, either covariance matrix Sigma or standard deviations SD and correlations rho must be given.

The sample size is calculated by simulating Wishart distributed random matrices, hence the results include a certain random variation.

Value

Object of class `power.mpe.test`, a list of arguments (including the computed one) augmented with method and note elements.

Note

The function first appeared in package **mpe**, which is now archived on CRAN.

Author(s)

Srinath Kolampally, Matthias Kohl <Matthias.Kohl@stamats.de>

References

Sugimoto, T. and Sozu, T. and Hamasaki, T. (2012). A convenient formula for sample size calculations in clinical trials with multiple co-primary continuous endpoints. *Pharmaceut. Statist.*, **11**: 118-128. doi:10.1002/pst.505

Sozu, T. and Sugimoto, T. and Hamasaki, T. and Evans, S.R. (2015). *Sample Size Determination in Clinical Trials with Multiple Endpoints*. Springer Briefs in Statistics, ISBN 978-3-319-22005-5.

See Also

`power.mpe.known.var`

Examples

```
## compute power
## Not run:
power.mpe.unknown.var(K = 2, n = 20, delta = c(1,1), Sigma = diag(c(1,1)))

## To compute sample size, first assume covariance as known
power.mpe.known.var(K = 2, delta = c(1,1), Sigma = diag(c(2,2)), power = 0.9,
                  sig.level = 0.025)

## The value of n, which is 51, is used as n.min and n.max must be larger
## then n.min so we try 60.
power.mpe.unknown.var(K = 2, delta = c(1,1), Sigma = diag(c(2,2)), power = 0.9,
                  sig.level = 0.025, n.min = 51, n.max = 60)

## More complex example with unknown covariance matrix assumed to be
Sigma <- matrix(c(1.440, 0.840, 1.296, 0.840,
                  0.840, 1.960, 0.168, 1.568,
                  1.296, 0.168, 1.440, 0.420,
                  0.840, 1.568, 0.420, 1.960), ncol = 4)
## compute power
power.mpe.unknown.var(K = 4, n = 90, delta = c(0.5, 0.75, 0.5, 0.75), Sigma = Sigma)
## equivalent: unknown SDs and correlation rho
power.mpe.unknown.var(K = 4, n = 90, delta = c(0.5, 0.75, 0.5, 0.75),
                      SD = c(1.2, 1.4, 1.2, 1.4),
                      rho = c(0.5, 0.9, 0.5, 0.1, 0.8, 0.25))
```

```
## End(Not run)
```

`power.nb.test` *Power Calculation for Comparing Two Negative Binomial Rates*

Description

Compute sample size or power for comparing two negative binomial rates.

Usage

```
power.nb.test(n = NULL, mu0, mu1, RR, duration = 1, theta, ssize.ratio = 1,
          sig.level = 0.05, power = NULL, alternative = c("two.sided", "one.sided"),
               approach = 3)
```

Arguments

`n`	Sample size for group 0 (control group).
`mu0`	expected rate of events per time unit for group 0
`mu1`	expected rate of events per time unit for group 1
`RR`	ratio of expected event rates: mu1/mu0
`duration`	(average) treatment duration
`theta`	theta parameter of negative binomial distribution; see `rnegbin`
`ssize.ratio`	ratio of sample sizes: n1/n where n1 is sample size of group 1
`sig.level`	Significance level (Type I error probability)
`power`	Power of test (1 minus Type II error probability)
`alternative`	one- or two-sided test
`approach`	1, 2, or 3; see Zhu and Lakkis (2014).

Details

Exactly one of the parameters `n` and `power` must be passed as `NULL`, and that parameter is determined from the other.

The computations are based on the formulas given in Zhu and Lakkis (2014). Please be careful, as we are using a slightly different parametrization (`theta` = 1/k).

Zhu and Lakkis (2014) based on their simulation studies recommend to use their approach 2 or 3.

Value

Object of class `"power.htest"`, a list of the arguments (including the computed one) augmented with a `note` element.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

H. Zhu and H. Lakkis (2014). Sample size calculation for comparing two negative binomial rates. *Statistics in Medicine*, **33**:376-387.

See Also

rnegbin, glm.nb

Examples

```
## examples from Table I in Zhu and Lakkis (2014)
## theta = 1/k, RR = rr, mu0 = r0, duration = mu_t
power.nb.test(mu0 = 0.8, RR = 0.85, theta = 1/0.4, duration = 0.75, power = 0.8, approach = 1)
power.nb.test(mu0 = 0.8, RR = 0.85, theta = 1/0.4, duration = 0.75, power = 0.8, approach = 2)
power.nb.test(mu0 = 0.8, RR = 0.85, theta = 1/0.4, duration = 0.75, power = 0.8, approach = 3)

power.nb.test(mu0 = 1.4, RR = 1.15, theta = 1/1.5, duration = 0.75, power = 0.8, approach = 1)
power.nb.test(mu0 = 1.4, RR = 1.15, theta = 1/1.5, duration = 0.75, power = 0.8, approach = 2)
power.nb.test(mu0 = 1.4, RR = 1.15, theta = 1/1.5, duration = 0.75, power = 0.8, approach = 3)


## examples from Table II in Zhu and Lakkis (2014) - seem to be total sample sizes
## can reproduce the results with mu_t = 1.0 (not 0.7!)
power.nb.test(mu0 = 2.0, RR = 0.5, theta = 1, duration = 1.0, ssize.ratio = 1,
              power = 0.8, approach = 1)
power.nb.test(mu0 = 2.0, RR = 0.5, theta = 1, duration = 1.0, ssize.ratio = 1,
              power = 0.8, approach = 2)
power.nb.test(mu0 = 2.0, RR = 0.5, theta = 1, duration = 1.0, ssize.ratio = 1,
              power = 0.8, approach = 3)

power.nb.test(mu0 = 10.0, RR = 1.5, theta = 1/5, duration = 1.0, ssize.ratio = 3/2,
              power = 0.8, approach = 1)
power.nb.test(mu0 = 10.0, RR = 1.5, theta = 1/5, duration = 1.0, ssize.ratio = 3/2,
              power = 0.8, approach = 2)
power.nb.test(mu0 = 10.0, RR = 1.5, theta = 1/5, duration = 1.0, ssize.ratio = 3/2,
              power = 0.8, approach = 3)


## examples from Table III in Zhu and Lakkis (2014)
power.nb.test(mu0 = 5.0, RR = 2.0, theta = 1/0.5, duration = 1, power = 0.8, approach = 1)
power.nb.test(mu0 = 5.0, RR = 2.0, theta = 1/0.5, duration = 1, power = 0.8, approach = 2)
power.nb.test(mu0 = 5.0, RR = 2.0, theta = 1/0.5, duration = 1, power = 0.8, approach = 3)


## examples from Table IV in Zhu and Lakkis (2014)
power.nb.test(mu0 = 5.9/3, RR = 0.4, theta = 0.49, duration = 3, power = 0.9, approach = 1)
power.nb.test(mu0 = 5.9/3, RR = 0.4, theta = 0.49, duration = 3, power = 0.9, approach = 2)
power.nb.test(mu0 = 5.9/3, RR = 0.4, theta = 0.49, duration = 3, power = 0.9, approach = 3)

power.nb.test(mu0 = 13/6, RR = 0.2, theta = 0.52, duration = 6, power = 0.9, approach = 1)
power.nb.test(mu0 = 13/6, RR = 0.2, theta = 0.52, duration = 6, power = 0.9, approach = 2)
power.nb.test(mu0 = 13/6, RR = 0.2, theta = 0.52, duration = 6, power = 0.9, approach = 3)
```

```
## see Section 5 of Zhu and Lakkis (2014)
power.nb.test(mu0 = 0.66, RR = 0.8, theta = 1/0.8, duration = 0.9, power = 0.9)
```

`power.prop1.test` *Power Calculations for One-Sample Test for Proportions*

Description

Compute the power of the one-sample test for proportions, or determine parameters to obtain a target power.

Usage

```
power.prop1.test(n = NULL, p1 = NULL, p0 = 0.5, sig.level = 0.05,
                                power = NULL,
                                alternative = c("two.sided", "less", "greater"),
                                cont.corr = TRUE, tol = .Machine$double.eps^0.25)
```

Arguments

`n`	number of observations (per group)
`p1`	expected probability
`p0`	probability under the null hypothesis
`sig.level`	significance level (Type I error probability)
`power`	power of test (1 minus Type II error probability)
`alternative`	one- or two-sided test. Can be abbreviated.
`cont.corr`	use continuity correction
`tol`	numerical tolerance used in root finding, the default providing (at least) four significant digits.

Details

Exactly one of the parameters `n`, `p1`, `power`, and `sig.level` must be passed as NULL, and that parameter is determined from the others. Notice that `sig.level` has a non-NULL default so `NULL` must be explicitly passed if you want it computed.

The computation is based on the asymptotic formulas provided in Section 2.5.1 of Fleiss et al. (2003). If `cont.corr = TRUE` a continuity correction is applied, which may lead to better approximations of the finite-sample values.

Value

Object of class `"power.htest"`, a list of the arguments (including the computed one) augmented with `method` and `note` elements.

Note

The documentation was adapted from power.prop.test.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

J.L. Fleiss, B. Levin and M.C. Paik (2003). *Statistical Methods for Rates and Proportions*. Wiley Series in Probability and Statistics.

See Also

power.prop.test, prop.test

Examples

```
power.prop1.test(p1 = 0.4, power = 0.8)
power.prop1.test(p1 = 0.4, power = 0.8, cont.corr = FALSE)
power.prop1.test(p1 = 0.6, power = 0.8)
power.prop1.test(n = 204, power = 0.8)
power.prop1.test(n = 204, p1 = 0.4, power = 0.8, sig.level = NULL)
power.prop1.test(n = 194, p1 = 0.4, power = 0.8, sig.level = NULL,
                 cont.corr = FALSE)

power.prop1.test(p1 = 0.1, p0 = 0.3, power = 0.8, alternative = "less")
power.prop1.test(p1 = 0.1, p0 = 0.3, power = 0.8, alternative = "less",
                 cont.corr = FALSE)
power.prop1.test(n = 31, p0 = 0.3, power = 0.8, alternative = "less")
power.prop1.test(n = 31, p1 = 0.1, p0 = 0.3, power = 0.8, sig.level = NULL,
                 alternative = "less")


power.prop1.test(p1 = 0.5, p0 = 0.3, power = 0.8, alternative = "greater")
power.prop1.test(p1 = 0.5, p0 = 0.3, power = 0.8, alternative = "greater",
                 cont.corr = FALSE)
power.prop1.test(n = 40, p0 = 0.3, power = 0.8, alternative = "greater")
power.prop1.test(n = 40, p1 = 0.5, p0 = 0.3, power = 0.8, sig.level = NULL,
                 alternative = "greater")
```

---

power.welch.t.test *Power Calculations for Two-sample Welch t Test*

Description

Compute the power of the two-sample Welch t test, or determine parameters to obtain a target power.

Usage

```
power.welch.t.test(n = NULL, delta = NULL, sd1 = 1, sd2 = 1, sig.level = 0.05,
                   power = NULL, alternative = c("two.sided", "one.sided"),
                   strict = FALSE, tol = .Machine$double.eps^0.25)
```

Arguments

n	number of observations (per group)
delta	(expected) true difference in means
sd1	(expected) standard deviation of group 1
sd2	(expected) standard deviation of group 2
sig.level	significance level (Type I error probability)
power	power of test (1 minus Type II error probability)
alternative	one- or two-sided test. Can be abbreviated.
strict	use strict interpretation in two-sided case
tol	numerical tolerance used in root finding, the default providing (at least) four significant digits.

Details

Exactly one of the parameters n, delta, power, sd1, sd2 and sig.level must be passed as NULL, and that parameter is determined from the others. Notice that the last three have non-NULL defaults, so NULL must be explicitly passed if you want to compute them.

If strict = TRUE is used, the power will include the probability of rejection in the opposite direction of the true effect, in the two-sided case. Without this the power will be half the significance level if the true difference is zero.

Value

Object of class "power.htest", a list of the arguments (including the computed one) augmented with method and note elements.

Note

The function and its documentation was adapted from power.t.test implemented by Peter Dalgaard and based on previous work by Claus Ekstroem.

uniroot is used to solve the power equation for unknowns, so you may see errors from it, notably about inability to bracket the root when invalid arguments are given.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

S.L. Jan and G. Shieh (2011). Optimal sample sizes for Welch's test under various allocation and cost considerations. *Behav Res Methods*, 43, 4:1014-22.

See Also

power.t.test, t.test, uniroot

Examples

```
## identical results as power.t.test, since sd = sd1 = sd2 = 1
power.welch.t.test(n = 20, delta = 1)
power.welch.t.test(power = .90, delta = 1)
power.welch.t.test(power = .90, delta = 1, alternative = "one.sided")

 ## sd1 = 0.5, sd2 = 1
power.welch.t.test(delta = 2, sd1 = 0.5, sd2 = 1, power = 0.9)


## empirical check
M <- 10000
pvals.welch <- numeric(M)
for(i in seq_len(M)){
  x <- rnorm(5, mean = 0, sd = 0.5)
  y <- rnorm(5, mean = 2, sd = 1.0)
  pvals.welch[i] <- t.test(x, y)$p.value
}
## empirical power
sum(pvals.welch < 0.05)/M
```

---

print.power.mpe.test *Print Methods for Hypothesis Tests, Sample size and Power Calculations*

Description

Printing objects of class "power.mpe.test" by simple print methods.

Usage

```
  ## S3 method for class 'power.mpe.test'
print(x, digits = getOption("digits"), ...)
```

Arguments

x	object of class "power.mpe.test".
digits	number of significant digits to be used.
...	further arguments to be passed to or from methods.

Details

The `print` method is based on the respective method `print.power.htest` of package **stats**.

A `power.mpe.test` object is just a named list of numbers and character strings, supplemented with `method` and `note` elements. The `method` is displayed as a title, the `note` as a footnote, and the remaining elements are given in an aligned 'name = value' format.

Value

the argument `x`, invisibly, as for all `print` methods.

Note

The function first appeared in package **mpe**, which is now archived on CRAN.

Author(s)

Srinath Kolampally, Matthias Kohl <Matthias.Kohl@stamats.de>

See Also

`print.power.htest`, `power.mpe.known.var`, `power.mpe.unknown.var`

Examples

```
(pkv <- power.mpe.known.var(K = 2, delta = c(1,1), Sigma = diag(c(2,2)), power = 0.9,
                            sig.level = 0.025))
print(pkv, digits =  4) # using less digits than default
print(pkv, digits = 12) # using more digits than default
```

---

qqunif *qq-Plots for Uniform Distribution*

Description

Produce qq-plot(s) of the given effect size and p values assuming a uniform distribution.

Usage

```
qqunif(x, ...)

## Default S3 method:
qqunif(x, min = 0, max = 1, ...)

## S3 method for class 'sim.power.ttest'
qqunif(x, color.line = "orange", shape = 19, size = 1,
                            alpha = 1, ...)
```

```
## S3 method for class 'sim.power.wtest'
qqunif(x, color.line = "orange", shape = 19, size = 1,
                            alpha = 1, ...)
```

Arguments

x	numeric vector or data (object).
min	single numeric, lower limit of the distribution.
max	single numeric, upper limit of the distribution.
color.line	color of the line indicating the uniform distribution.
shape	point shape.
size	point size.
alpha	bleding factor (default: no blending.
...	further arguments that may be passed through).

Details

The plot generates a ggplot2 object that is shown.

Missing values are handled by the ggplot2 functions.

Value

Object of class gg and ggplot.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

Examples

```
## default
qqunif(runif(100))

## visualization of empirical power and type-I-error
res1 <- sim.power.t.test(nx = 5, rx = rnorm, rx.H0 = rnorm,
                         ny = 10, ry = function(x) rnorm(x, mean = 3, sd = 3),
                         ry.H0 = function(x) rnorm(x, sd = 3))
qqunif(res1, alpha = 0.1)

res2 <- sim.power.wilcox.test(nx = 6, rx = rnorm, rx.H0 = rnorm,
                      ny = 6, ry = function(x) rnorm(x, mean = 2),
                      ry.H0 = rnorm)
qqunif(res2)
```

`sim.power.t.test` *Monte Carlo Simulations for Empirical Power of Two-sample t-Tests*

Description

Simulate the empirical power and type-I-error of two-sample t-tests; i.e., classical (equal variances), Welch and Hsu t-tests.

Usage

```
sim.power.t.test(nx, rx, rx.H0 = NULL, ny, ry, ry.H0 = NULL,
                 sig.level = 0.05, conf.int = FALSE, mu = 0,
                 alternative = c("two.sided", "less", "greater"),
                 iter = 10000)
```

Arguments

`nx`	single numeric, sample size of first group.
`rx`	function to simulate the values of first group (assuming H1).
`rx.H0`	`NULL` or function to simulate the values of first group (assuming H0).
`ny`	single numeric, sample size of second group.
`ry`	function to simulate the values of second group (assuming H1).
`ry.H0`	`NULL` or function to simulate the values of second group (assuming H0).
`sig.level`	significance level (type I error probability)
`conf.int`	logical, shall confidence intervals be computed. Increases computation time!
`mu`	true value of the location shift for the null hypothesis.
`alternative`	one- or two-sided test. Can be abbreviated.
`iter`	single integer, number of interations of the simulations.

Details

Functions `rx` and `ry` are used to simulate the data under the alternative hypothesis H1. If specified, functions `rx.H0` and `ry.H0` simulte the data unter the null hypothesis H0.

For fast computations functions from package `matrixTests` are used.

Value

Object of class `"sim.power.ttest"` with the results of the three t-tests in the list elements `Classical`, `Welch` and `Hsu`. In addition, the simulation setup is saved in element `SetUp`.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

J. Hedderich, L. Sachs. *Angewandte Statistik: Methodensammlung mit R*. Springer 2018.

Hsu, P. (1938). Contribution to the theory of "student's" t-test as applied to the problem of two samples. *Statistical Research Memoirs* **2**: 1-24.

Student (1908). The Probable Error of a Mean. *Biometrika*, **6**(1): 1-25.

Welch, B. L. (1947). The generalization of "Student's" problem when several different population variances are involved. *Biometrika*, **34** (1-2): 28-35.

See Also

`t.test`, `hsu.t.test`, `ttest`

Examples

```
## Equal variance, small sample size
power.t.test(n = 5, delta = 2)
power.welch.t.test(n = 5, delta = 2)
power.hsu.t.test(n = 5, delta = 2)
sim.power.t.test(nx = 5, rx = rnorm, rx.H0 = rnorm,
                 ny = 5, ry = function(x) rnorm(x, mean = 2), ry.H0 = rnorm)

## Equal variance, moderate sample size
power.t.test(n = 25, delta = 0.8)
power.welch.t.test(n = 25, delta = 0.8)
power.hsu.t.test(n = 25, delta = 0.8)
sim.power.t.test(nx = 25, rx = rnorm, rx.H0 = rnorm,
                 ny = 25, ry = function(x) rnorm(x, mean = 0.8), ry.H0 = rnorm)

## Equal variance, high sample size
power.t.test(n = 100, delta = 0.4)
power.welch.t.test(n = 100, delta = 0.4)
power.hsu.t.test(n = 100, delta = 0.4)
sim.power.t.test(nx = 100, rx = rnorm, rx.H0 = rnorm,
                 ny = 100, ry = function(x) rnorm(x, mean = 0.4), ry.H0 = rnorm)

## Unequal variance, small sample size
power.welch.t.test(n = 5, delta = 5, sd1 = 1, sd2 = 3)
power.hsu.t.test(n = 5, delta = 5, sd1 = 1, sd2 = 3)
sim.power.t.test(nx = 5, rx = rnorm, rx.H0 = rnorm,
                 ny = 5, ry = function(x) rnorm(x, mean = 5, sd = 3),
                 ry.H0 = function(x) rnorm(x, sd = 3))

## Unequal variance, moderate sample size
power.welch.t.test(n = 25, delta = 1.8, sd1 = 1, sd2 = 3)
power.hsu.t.test(n = 25, delta = 1.8, sd1 = 1, sd2 = 3)
sim.power.t.test(nx = 25, rx = rnorm, rx.H0 = rnorm,
                 ny = 25, ry = function(x) rnorm(x, mean = 1.8, sd = 3),
                 ry.H0 = function(x) rnorm(x, sd = 3))

## Unequal variance, high sample size
```

```
power.welch.t.test(n = 100, delta = 0.9, sd1 = 1, sd2 = 3)
power.hsu.t.test(n = 100, delta = 0.9, sd1 = 1, sd2 = 3)
sim.power.t.test(nx = 100, rx = rnorm, rx.H0 = rnorm,
                 ny = 100, ry = function(x) rnorm(x, mean = 0.9, sd = 3),
                 ry.H0 = function(x) rnorm(x, sd = 3))

## Unequal variance, unequal sample sizes
## small sample sizes
sim.power.t.test(nx = 10, rx = rnorm, rx.H0 = rnorm,
                 ny = 5, ry = function(x) rnorm(x, mean = 5, sd = 3),
                 ry.H0 = function(x) rnorm(x, sd = 3))
sim.power.t.test(nx = 5, rx = rnorm, rx.H0 = rnorm,
                 ny = 10, ry = function(x) rnorm(x, mean = 3, sd = 3),
                 ry.H0 = function(x) rnorm(x, sd = 3))

## Unequal variance, unequal sample sizes
## moderate sample sizes
sim.power.t.test(nx = 25, rx = rnorm, rx.H0 = rnorm,
                 ny = 50, ry = function(x) rnorm(x, mean = 1.5, sd = 3),
                 ry.H0 = function(x) rnorm(x, sd = 3))

## Unequal variance, unequal sample sizes
## high sample sizes
sim.power.t.test(nx = 100, rx = rnorm, rx.H0 = rnorm,
                 ny = 200, ry = function(x) rnorm(x, mean = 0.6, sd = 3),
                 ry.H0 = function(x) rnorm(x, sd = 3))
```

`sim.power.wilcox.test` *Monte Carlo Simulations for Empirical Power of Wilcoxon-Mann-Whitney Tests*

Description

Simulate the empirical power and type-I-error of Wilcoxon-Mann-Whitney tests.

Usage

```
sim.power.wilcox.test(nx, rx, rx.H0 = NULL, ny, ry, ry.H0 = NULL,
                      alternative = c("two.sided", "less", "greater"),
                      sig.level = 0.05, conf.int = FALSE, approximate = FALSE,
                      ties = FALSE, iter = 10000, nresample = 10000,
                      parallel = "no", ncpus = 1L, cl = NULL)
```

Arguments

`nx`	single numeric, sample size of first group.
`rx`	function to simulate the values of first group (assuming H1).
`rx.H0`	`NULL` or function to simulate the values of first group (assuming H0).

ny	single numeric, sample size of second group.
ry	function to simulate the values of second group (assuming H1).
ry.H0	NULL or function to simulate the values of second group (assuming H0).
alternative	one- or two-sided test. Can be abbreviated.
sig.level	significance level (type I error probability)
conf.int	logical, shall confidence intervals be computed. Strongly increases computation time!
approximate	logical, shall an approximate test be computed; see LocationTests. Increases computation time!
ties	logical, indicating whether ties may occur. Increases computation time!
iter	single positive integer, number of interations of the simulations.
nresample	single positive integer, the number of Monte Carlo replicates used for the computation of the approximative reference distribution; see NullDistribution.
parallel	a character, the type of parallel operation: either "no" (default), "multicore" or "snow"; see NullDistribution.
ncpus	a single integer, the number of processes to be used in parallel operation. Defaults to 1L; see NullDistribution.
cl	an object inheriting from class "cluster", specifying an optional parallel or snow cluster if parallel = "snow". Defaults to NULL; see NullDistribution.

Details

Functions rx and ry are used to simulate the data under the alternative hypothesis H1. If specified, functions rx.H0 and ry.H0 simulte the data unter the null hypothesis H0.

For fast computations functions from package matrixTests and package coin are used.

Value

Object of class "sim.power.wtest" with the results of the Wilcoxon-Mann-Whitney tests. A list elements Exact, Asymptotic and Approximate. In addition, the simulation setup is saved in element SetUp.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Mann, H and Withney, D (1947). On a test of whether one of two random variables is stochastically larger than the other. *Annals of mathematical Statistics*, **18**, 50-60.

Wilcoxon, F (1945). Individual Comparisons by Ranking Methods. *Biometrics Bulletin*, **1**, 80-83.

See Also

wilcox.test, LocationTests, wilcoxon

Examples

```
## Equal variance, small sample size
power.t.test(n = 5, power = 0.8)
sim.ssize.wilcox.test(rx = rnorm, ry = function(x) rnorm(x, mean = 2),
                      power = 0.8, n.min = 3, n.max = 10, step.size = 1)
sim.power.wilcox.test(nx = 6, rx = rnorm, rx.H0 = rnorm,
                      ny = 6, ry = function(x) rnorm(x, mean = 2),
                      ry.H0 = rnorm)
```

---

sim.ssize.wilcox.test *Sample Size for Wilcoxon Rank Sum and Signed Rank Tests*

Description

Simulate the empirical power of Wilcoxon rank sum and signed rank tests for computing the required sample size.

Usage

```
sim.ssize.wilcox.test(rx, ry = NULL, mu = 0, sig.level = 0.05, power = 0.8,
                      type = c("two.sample", "one.sample", "paired"),
                      alternative = c("two.sided", "less", "greater"),
                      n.min = 10, n.max = 200, step.size = 10,
                      iter = 10000, BREAK = TRUE, exact = NA, correct = TRUE)
```

Arguments

rx	function to simulate the values of x, respectively x-y in the paired case.
ry	function to simulate the values of y in the two-sample case
mu	true values of the location shift for the null hypothesis.
sig.level	significance level (Type I error probability)
power	two-sample, one-sample or paired test
type	one- or two-sided test. Can be abbreviated.
alternative	one- or two-sided test. Can be abbreviated.
n.min	integer, start value of grid search.
n.max	integer, stop value of grid search.
step.size	integer, step size used in the grid search.
iter	integer, number of interations of the simulations.
BREAK	logical, grid search stops when the emperical power is larger than the requested power.
exact	logical or NA (default) indicator whether an exact p-value should be computed (see Details at wilcoxon). A single value or a logical vector with values for each observation.
correct	ogical indicator whether continuity correction should be applied in the cases where p-values are obtained using normal approximation. A single value or logical vector with values for each observation; see wilcoxon.

Details

Functions `rx` and `ry` are used to simulate the data and functions `row_wilcoxon_twosample` and `row_wilcoxon_onesample` of package **matrixTests** are used to efficiently compute the p values of the respective test.

We recommend a two steps procedure: In the first step, start with a wide grid and find out in which range of sample size values the intended power will be achieved. In the second step, the interval identified in the first step is used to find the sample size that leads to the required power setting `step.size = 1` and `BREAK = FALSE`. This approach is applied in the examples below.

Value

Object of class `"power.htest"`, a list of the arguments (including the computed one) augmented with `method` and `note` elements.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Wilcoxon, F (1945). Individual Comparisons by Ranking Methods. *Biometrics Bulletin*, **1**, 80-83.

See Also

`wilcox.test`, `wilcoxon`

Examples

```
##############################################################################
## two-sample
## iter = 1000 to reduce check time
##############################################################################
rx <- function(n) rnorm(n, mean = 0, sd = 1)
ry <- function(n) rnorm(n, mean = 0.5, sd = 1)
sim.ssize.wilcox.test(rx = rx, ry = ry, n.max = 100, iter = 1000)
sim.ssize.wilcox.test(rx = rx, ry = ry, n.min = 65, n.max = 70, step.size = 1,
                      iter = 1000, BREAK = FALSE)
## compared to
power.t.test(delta = 0.5, power = 0.8)

rx <- function(n) rnorm(n, mean = 0, sd = 1)
ry <- function(n) rnorm(n, mean = 0.5, sd = 1.5)
sim.ssize.wilcox.test(rx = rx, ry = ry, n.max = 100, iter = 1000, alternative = "less")
sim.ssize.wilcox.test(rx = rx, ry = ry, n.min = 85, n.max = 90, step.size = 1,
                      iter = 1000, BREAK = FALSE, alternative = "less")
## compared to
power.welch.t.test(delta = 0.5, sd = 1, sd2 = 1.5, power = 0.8, alternative = "one.sided")

rx <- function(n) rnorm(n, mean = 0.5, sd = 1)
ry <- function(n) rnorm(n, mean = 0, sd = 1)
```

```
sim.ssize.wilcox.test(rx = rx, ry = ry, n.max = 100, iter = 1000, alternative = "greater")
sim.ssize.wilcox.test(rx = rx, ry = ry, n.min = 50, n.max = 55, step.size = 1,
                      iter = 1000, BREAK = FALSE, alternative = "greater")
## compared to
power.t.test(delta = 0.5, power = 0.8, alternative = "one.sided")

rx <- function(n) rgamma(n, scale = 10, shape = 1)
ry <- function(n) rgamma(n, scale = 15, shape = 1)
sim.ssize.wilcox.test(rx = rx, ry = ry, n.max = 200, iter = 1000)
sim.ssize.wilcox.test(rx = rx, ry = ry, n.min = 125, n.max = 135, step.size = 1,
                      iter = 1000, BREAK = FALSE)

################################################################################
## one-sample
## iter = 1000 to reduce check time
################################################################################
rx <- function(n) rnorm(n, mean = 0.5, sd = 1)
sim.ssize.wilcox.test(rx = rx, mu = 0, type = "one.sample", n.max = 100, iter = 1000)
sim.ssize.wilcox.test(rx = rx, mu = 0, type = "one.sample", n.min = 33, n.max = 38,
                      step.size = 1, iter = 1000, BREAK = FALSE)
## compared to
power.t.test(delta = 0.5, power = 0.8, type = "one.sample")

sim.ssize.wilcox.test(rx = rx, mu = 0, type = "one.sample", n.max = 100, iter = 1000,
                      alternative = "greater")
sim.ssize.wilcox.test(rx = rx, mu = 0, type = "one.sample", n.min = 25, n.max = 30,
                     step.size = 1, iter = 1000, BREAK = FALSE, alternative = "greater")
## compared to
power.t.test(delta = 0.5, power = 0.8, type = "one.sample", alternative = "one.sided")

sim.ssize.wilcox.test(rx = rx, mu = 1, type = "one.sample", n.max = 100, iter = 1000,
                      alternative = "less")
sim.ssize.wilcox.test(rx = rx, mu = 1, type = "one.sample", n.min = 20, n.max = 30,
                      step.size = 1, iter = 1000, BREAK = FALSE, alternative = "less")
## compared to
power.t.test(delta = 0.5, power = 0.8, type = "one.sample", alternative = "one.sided")

rx <- function(n) rgamma(n, scale = 10, shape = 1)
sim.ssize.wilcox.test(rx = rx, mu = 5, type = "one.sample", n.max = 200, iter = 1000)
sim.ssize.wilcox.test(rx = rx, mu = 5, type = "one.sample", n.min = 40, n.max = 50,
                      step.size = 1, iter = 1000, BREAK = FALSE)

################################################################################
## paired
## identical to one-sample, requires random number generating function
## that simulates the difference x-y
## iter = 1000 to reduce check time
################################################################################
rxy <- function(n) rnorm(n, mean = 0.5, sd = 1)
sim.ssize.wilcox.test(rx = rxy, mu = 0, type = "paired", n.max = 100,
                      iter = 1000)
sim.ssize.wilcox.test(rx = rxy, mu = 0, type = "paired", n.min = 33,
                      n.max = 38, step.size = 1, iter = 1000, BREAK = FALSE)
```

```
## compared to
power.t.test(delta = 0.5, power = 0.8, type = "paired")
```

---

ssize.pcc *Sample Size Planning for Developing Classifiers Using High Dimensional Data*

Description

Calculate sample size for training set in developing classifiers using high dimensional data. The calculation is based on the probability of correct classification (PCC).

Usage

```
ssize.pcc(gamma, stdFC, prev = 0.5, nrFeatures, sigFeatures = 20, verbose = FALSE)
```

Arguments

gamma	tolerance between PCC(infty) and PCC(n).
stdFC	expected standardized fold-change; that is, expected fold-change devided by within class standard deviation.
prev	expected prevalence.
nrFeatures	number of features (variables) considered.
sigFeatures	number of significatn features; default (20) should be sufficient for most if not all cases.
verbose	print intermediate results.

Details

The computations are based the algorithm provided in Section~4.2 of Dobbin and Simon (2007). Prevalence is incorporated by the simple rough approach given in Section~4.4 (ibid.).

The results for prevalence equal to $50%$ are identical to the numbers computed by https://brb.nci.nih.gov/brb/samplesize/samplesize4GE.html. For other prevalences the numbers differ and are larger for our implementation.

Value

Object of class "power.htest", a list of the arguments (including the computed one) augmented with method and note elements.

Note

optimize is used to solve equation (4.3) of Dobbin and Simon (2007), so you may see errors from it.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

K. Dobbin and R. Simon (2007). Sample size planning for developing classifiers using high-dimensional DNA microarray data. *Biostatistics*, **8**(1):101-117.

K. Dobbin, Y. Zhao, R. Simon (2008). How Large a Training Set is Needed to Develop a Classifier for Microarray Data? *Clin Cancer Res.*, **14**(1):108-114.

See Also

optimize

Examples

```
## see Table 2 of Dobbin et al. (2008)
g <- 0.1
fc <- 1.6
ssize.pcc(gamma = g, stdFC = fc, nrFeatures = 22000)

## see Table 3 of Dobbin et al. (2008)
g <- 0.05
fc <- 1.1
ssize.pcc(gamma = g, stdFC = fc, nrFeatures = 22000)
```

---

ssize.propCI *Sample Size Calculation for Confidence Interval of a Proportion*

Description

Compute the sample size for the two-sided confidence interval of a single proportion.

Usage

```
ssize.propCI(prop, width, conf.level = 0.95,  method = "wald-cc")
```

Arguments

prop	expected proportion
width	width of the confidence interval
conf.level	confidence level
method	method used to compute the confidence interval; see Details.

Details

The computation is based on the asymptotic formulas provided in Section 2.5.2 of Fleiss et al. (2003). If `method = "wald-cc"` a continuity correction is applied.

There are also methods for Jeffreys, Clopper-Pearson, Wilson and the Agresti-Coull interval; see also `binomCI`.

Value

Object of class `"power.htest"`, a list of the arguments (including the computed one) augmented with `method` and `note` elements.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

J.L. Fleiss, B. Levin and M.C. Paik (2003). *Statistical Methods for Rates and Proportions*. Wiley Series in Probability and Statistics.

W.W. Piegorsch (2004). Sample sizes for improved binomial confidence intervals. *Computational Statistics & Data Analysis*, **46**, 309-316.

M. Thulin (2014). The cost of using exact confidence intervals for a binomial proportion. *Electronic Journal of Statistics*, **8**(1), 817-840.

See Also

`power.prop1.test`, `binomCI`

Examples

```
ssize.propCI(prop = 0.1, width = 0.1)
ssize.propCI(prop = 0.3, width = 0.1)
ssize.propCI(prop = 0.3, width = 0.1, method = "wald")
ssize.propCI(prop = 0.3, width = 0.1, method = "jeffreys")
ssize.propCI(prop = 0.3, width = 0.1, method = "clopper-pearson")
ssize.propCI(prop = 0.3, width = 0.1, method = "wilson")
ssize.propCI(prop = 0.3, width = 0.1, method = "agresti-coull")
```

---

ssize.reference.range *Power Calculations for Two-sample Hsu t Test*

Description

Compute the sample size for reference range studies, or determine parameters for a given sample size; see Jennen-Steinmetz and Wellek (2005).

Usage

```
ssize.reference.range(n = NULL, delta = NULL, ref.prob = 0.95, conf.prob = NULL,
                      alternative = c("two.sided", "one.sided"),
                      method = "parametric", exact = TRUE,
                      tol = .Machine$double.eps^0.5)
```

Arguments

n	number of observations
delta	difference between empirical and target coverage of reference range
ref.prob	target coverage of reference range
conf.prob	confidence probability to acchieve given difference between empirical and target coverage
alternative	a character string specifying "two.sided" (default), or one-sided reference ranges. You can specify just the initial letter.
method	either "parametric" or "nonparametric"; see details
exact	use exact or approximate method
tol	numerical tolerance used in root finding, the default providing (at least) eight significant digits.

Details

Exactly one of the parameters n, delta, ref.prob and conf.prob must be passed as NULL, and that parameter is determined from the others. In case of ref.prob NULL must be explicitly passed if you want to compute it.

If method "parametric" a normal distribution is assumed for the investigated quantity.

If method "nonparametric" an arbitrary continuous probability distribution is assumed.

If exact = TRUE is used, the computations use the exact formulas (5) and (9) of Jennen-Steinmetz and Wellek (2005).

If exact = FALSE is used, the computations use the approximate formulas (6) and (10) of Jennen-Steinmetz and Wellek (2005).

Value

Object of class "power.htest", a list of the arguments (including the computed one) augmented with method and note elements.

Note

uniroot is used to solve the equations for unknowns, so you may see errors from it, notably about inability to bracket the root when invalid arguments are given.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

C. Jennen-Steinmetz, S. Wellek (2005). A new approach to sample size calculation for reference interval studies. *Statistics in Medicine* 24:3199-3212.

See Also

uniroot

Examples

```
## see Table 1 in Jennen-Steinmetz and Wellek (2005)
ssize.reference.range(delta = 0.03, ref.prob = 0.9, conf.prob = 0.9,
                      method = "parametric", exact = TRUE)
## 135 vs 125 (error in Table 1)
ssize.reference.range(delta = 0.03, ref.prob = 0.9, conf.prob = 0.9,
                      method = "nonparametric", exact = TRUE)
ssize.reference.range(delta = 0.03, ref.prob = 0.9, conf.prob = 0.9,
                      method = "parametric", exact = FALSE)
ssize.reference.range(delta = 0.03, ref.prob = 0.9, conf.prob = 0.9,
                      method = "nonparametric", exact = FALSE)

ssize.reference.range(delta = 0.025, ref.prob = 0.9, conf.prob = 0.9,
                      method = "parametric", exact = TRUE)
ssize.reference.range(delta = 0.025, ref.prob = 0.9, conf.prob = 0.9,
                      method = "nonparametric", exact = TRUE)
ssize.reference.range(delta = 0.025, ref.prob = 0.9, conf.prob = 0.9,
                      method = "parametric", exact = FALSE)
ssize.reference.range(delta = 0.025, ref.prob = 0.9, conf.prob = 0.9,
                      method = "nonparametric", exact = FALSE)

ssize.reference.range(delta = 0.02, ref.prob = 0.9, conf.prob = 0.9,
                      method = "parametric", exact = TRUE)
## 314 vs. 305 (error Table 1?)
ssize.reference.range(delta = 0.02, ref.prob = 0.9, conf.prob = 0.9,
                      method = "nonparametric", exact = TRUE)
ssize.reference.range(delta = 0.02, ref.prob = 0.9, conf.prob = 0.9,
                      method = "parametric", exact = FALSE)
ssize.reference.range(delta = 0.02, ref.prob = 0.9, conf.prob = 0.9,
                      method = "nonparametric", exact = FALSE)

ssize.reference.range(delta = 0.015, ref.prob = 0.9, conf.prob = 0.9,
                      method = "parametric", exact = TRUE)
ssize.reference.range(delta = 0.015, ref.prob = 0.9, conf.prob = 0.9,
                      method = "nonparametric", exact = TRUE)
ssize.reference.range(delta = 0.015, ref.prob = 0.9, conf.prob = 0.9,
                      method = "parametric", exact = FALSE)
ssize.reference.range(delta = 0.015, ref.prob = 0.9, conf.prob = 0.9,
                      method = "nonparametric", exact = FALSE)

ssize.reference.range(delta = 0.01, ref.prob = 0.9, conf.prob = 0.9,
                      method = "parametric", exact = TRUE)
ssize.reference.range(delta = 0.01, ref.prob = 0.9, conf.prob = 0.9,
```

```
                      method = "nonparametric", exact = TRUE)
ssize.reference.range(delta = 0.01, ref.prob = 0.9, conf.prob = 0.9,
                      method = "parametric", exact = FALSE)
ssize.reference.range(delta = 0.01, ref.prob = 0.9, conf.prob = 0.9,
                      method = "nonparametric", exact = FALSE)

ssize.reference.range(delta = 0.015, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = TRUE)
ssize.reference.range(delta = 0.015, ref.prob = 0.95, conf.prob = 0.9,
                      method = "nonparametric", exact = TRUE)
ssize.reference.range(delta = 0.015, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = FALSE)
ssize.reference.range(delta = 0.015, ref.prob = 0.95, conf.prob = 0.9,
                      method = "nonparametric", exact = FALSE)

ssize.reference.range(delta = 0.0125, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = TRUE)
ssize.reference.range(delta = 0.0125, ref.prob = 0.95, conf.prob = 0.9,
                      method = "nonparametric", exact = TRUE)
ssize.reference.range(delta = 0.0125, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = FALSE)
ssize.reference.range(delta = 0.0125, ref.prob = 0.95, conf.prob = 0.9,
                      method = "nonparametric", exact = FALSE)

ssize.reference.range(delta = 0.01, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = TRUE)
ssize.reference.range(delta = 0.01, ref.prob = 0.95, conf.prob = 0.9,
                      method = "nonparametric", exact = TRUE)
ssize.reference.range(delta = 0.01, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = FALSE)
ssize.reference.range(delta = 0.01, ref.prob = 0.95, conf.prob = 0.9,
                      method = "nonparametric", exact = FALSE)

ssize.reference.range(delta = 0.0075, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = TRUE)
ssize.reference.range(delta = 0.0075, ref.prob = 0.95, conf.prob = 0.9,
                      method = "nonparametric", exact = TRUE)
ssize.reference.range(delta = 0.0075, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = FALSE)
ssize.reference.range(delta = 0.0075, ref.prob = 0.95, conf.prob = 0.9,
                      method = "nonparametric", exact = FALSE)

ssize.reference.range(delta = 0.005, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = TRUE)
ssize.reference.range(delta = 0.005, ref.prob = 0.95, conf.prob = 0.9,
                      method = "nonparametric", exact = TRUE)
ssize.reference.range(delta = 0.005, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = FALSE)
ssize.reference.range(delta = 0.005, ref.prob = 0.95, conf.prob = 0.9,
                      method = "nonparametric", exact = FALSE)


## results are equivalent to one-sided reference range with coverage of
```

```
## 95 percent instead of 90 percent; for example
ssize.reference.range(delta = 0.03, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = TRUE, alternative = "one.sided")
## 135 vs 125 (error in Table 1)
ssize.reference.range(delta = 0.03, ref.prob = 0.95, conf.prob = 0.9,
                     method = "nonparametric", exact = TRUE, alternative = "one.sided")
ssize.reference.range(delta = 0.03, ref.prob = 0.95, conf.prob = 0.9,
                      method = "parametric", exact = FALSE, alternative = "one.sided")
ssize.reference.range(delta = 0.03, ref.prob = 0.95, conf.prob = 0.9,
                    method = "nonparametric", exact = FALSE, alternative = "one.sided")
```

`volcano` *Volcano Plots*

Description

Produce volcano plot(s) for simulations of power and type-I-error of tests.

Usage

```
## S3 method for class 'sim.power.ttest'
volcano(x, alpha = 1, shape = 19,
                                    hex = FALSE, bins = 50, ...)

## S3 method for class 'sim.power.wtest'
volcano(x, alpha = 1, shape = 19,
                                    hex = FALSE, bins = 50, ...)
```

Arguments

`x`	object of class `sim.power.ttest`.
`alpha`	bleding factor (default: no blending.
`shape`	point shape used.
`hex`	logical, should hexagonal binning be used.
`bins`	number of bins used for hexagonal binning.
`...`	further arguments that may be passed through).

Details

The plot generates a `ggplot2` object that is shown.

Missing values are handled by the `ggplot2` functions.

Value

Object of class gg and `ggplot`.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Wikipedia contributors, *Volcano plot (statistics)*, Wikipedia, The Free Encyclopedia, https://en.wikipedia.org/w/index.php?title=Volcano_plot_(statistics)&oldid=900217316 (accessed December 25, 2019).

For more sophisticated and flexible volcano plots see for instance: Blighe K, Rana S, Lewis M (2019). EnhancedVolcano: Publication-ready volcano plots with enhanced colouring and labeling. R/Bioconductor package. https://github.com/kevinblighe/EnhancedVolcano.

See Also

volcano

Examples

```
res1 <- sim.power.t.test(nx = 5, rx = rnorm, rx.H0 = rnorm,
                         ny = 10, ry = function(x) rnorm(x, mean = 3, sd = 3),
                         ry.H0 = function(x) rnorm(x, sd = 3))
volcano(res1)

## low number of iterations to reduce computation time
res2 <- sim.power.wilcox.test(nx = 6, rx = rnorm, rx.H0 = rnorm,
                        ny = 6, ry = function(x) rnorm(x, mean = 2),
                        ry.H0 = rnorm, iter = 100, conf.int = TRUE)
volcano(res2)
```

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