

# Package ‘ETRep’

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**Type** Package

**Title** Analysis of Elliptical Tubes Under the Relative Curvature Condition

**Version** 0.1.0

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**Description** Analysis of elliptical tubes with applications in biological modeling. The package is based on the references: Taheri, M., Pizer, S. M., & Schulz, J. (2024) ``The Mean Shape under the Relative Curvature Condition." arXiv <doi:10.48550/arXiv.2404.01043>. Mohsen Taheri Shalmani (2024) ``Shape Statistics via Skeletal Structures", PhD Thesis, University of Stavanger, Norway <doi:10.13140/RG.2.2.34500.23685>. Key features include constructing discrete elliptical tubes, calculating transformations, validating structures under the Relative Curvature Condition, computing means, and generating simulations. Supports intrinsic and non-intrinsic mean calculations and transformations, size estimation, plotting, and random sample generation based on a reference tube.

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**URL** [https://github.com/MohsenTaheriShalmani/Elliptical\\_Tubes](https://github.com/MohsenTaheriShalmani/Elliptical_Tubes)

**Depends** R (>= 4.0.0)

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check\_Tube\_Legality    *Check the Legality of an Elliptical Tube (ETRep)*

---

### Description

Checks the validity of a given ETRep based on the Relative Curvature Condition (RCC) and principal radii such that for all  $i$   $a_i > b_i$ .

### Usage

```
check_Tube_Legality(tube)
```

### Arguments

tube                    List containing ETRep details.

### Value

Logical value: TRUE if valid, FALSE otherwise.

### Examples

```
# Load tube
data("colon3D")
check_Tube_Legality(tube = colon3D)
```

---

`colon3D`*Data*

---

**Description**

A colon sample as an elliptical tube.

**Usage**

```
colon3D
```

**Format**

A list containing the information of an e-tube

**Source**

Generated and stored in the package's 'data/' folder.

---

`create_Elliptical_Tube`*Create a Discrete Elliptical Tube (ETRep)*

---

**Description**

Constructs a discrete elliptical tube (ETRep) based on specified parameters.

**Usage**

```
create_Elliptical_Tube(  
  numberOfFrames,  
  method,  
  materialFramesBasedOnParents = NA,  
  initialFrame = diag(3),  
  initialPoint = c(0, 0, 0),  
  EulerAngles_Matrix = NA,  
  ellipseResolution = 10,  
  ellipseRadii_a,  
  ellipseRadii_b,  
  connectionsLengths,  
  plotting = TRUE,  
  add = FALSE  
)
```

**Arguments**

numberOfFrames	Integer, specifies the number of consecutive material frames.
method	String, either "basedOnEulerAngles" or "basedOnMaterialFrames", defines the material frames method.
materialFramesBasedOnParents	Array (3 x 3 x numberOfFrames) with pre-defined material frames.
initialFrame	Matrix 3 x 3 as the initial frame
initialPoint	Real vector with three elements as the initial point
EulerAngles_Matrix	Matrix of dimensions numberOfFrames x 3 with Euler angles to define material frames.
ellipseResolution	Integer, resolution of elliptical cross-sections (default is 10).
ellipseRadii_a	Numeric vector for the primary radii of cross-sections.
ellipseRadii_b	Numeric vector for the secondary radii of cross-sections.
connectionsLengths	Numeric vector for lengths of spinal connection vectors.
plotting	Logical, enables plotting of the ETRep (default is TRUE).
add	Logical, enables overlay plotting

**Value**

List containing tube details (orientation, radii, connection lengths, boundary points, etc.).

**Examples**

```

numberOfFrames<-15
EulerAngles_alpha<-c(rep(0,numberOfFrames))
EulerAngles_beta<-c(rep(-pi/20,numberOfFrames))
EulerAngles_gamma<-c(rep(0,numberOfFrames))
EulerAngles_Matrix<-cbind(EulerAngles_alpha,
                           EulerAngles_beta,
                           EulerAngles_gamma)
tube <- create_Elliptical_Tube(numberOfFrames = numberOfFrames,
                              method = "basedOnEulerAngles",
                              EulerAngles_Matrix = EulerAngles_Matrix,
                              ellipseResolution = 10,
                              ellipseRadii_a = rep(3, numberOfFrames),
                              ellipseRadii_b = rep(2, numberOfFrames),
                              connectionsLengths = rep(4, numberOfFrames),
                              plotting = FALSE)

# Plotting
plot_Elliptical_Tube(tube = tube,plot_frames = FALSE,
                    plot_skeletal_sheet = TRUE,
                    plot_r_project = FALSE,
                    plot_r_max = FALSE,add = FALSE)

```

---

`intrinsic_Distance_Between2tubes`*Calculating the intrinsic distance between two ETReps*

---

**Description**

Calculating the intrinsic distance between two ETReps

**Usage**

```
intrinsic_Distance_Between2tubes(tube1, tube2)
```

**Arguments**

tube1	List containing ETRep details.
tube2	List containing ETRep details.

**Value**

Numeric

**Examples**

```
# Load tubes
data("tube_A")
data("tube_B")
intrinsic_Distance_Between2tubes(tube1 = tube_A, tube2 = tube_B)
```

---

`intrinsic_mean_tube` *Calculate Intrinsic Mean of ETReps*

---

**Description**

Computes the intrinsic mean of a set of ETReps.

**Usage**

```
intrinsic_mean_tube(tubes, type = "sizeAndShapeAnalysis", plotting = TRUE)
```

**Arguments**

tubes	List of ETReps.
type	String, "ShapeAnalysis" or "sizeAndShapeAnalysis" (default is "sizeAndShapeAnalysis").
plotting	Logical, enables visualization of the mean (default is TRUE).

**Value**

List representing the mean ETRep.

**Examples**

```
#Example 1
# Load tubes
data("tube_A")
data("tube_B")
intrinsic_mean<-
  intrinsic_mean_tube(tubes = list(tube_A,tube_B),
                    plotting = FALSE)

# Plotting
plot_Elliptical_Tube(tube = intrinsic_mean,
                    plot_frames = FALSE,
                    plot_skeletal_sheet = FALSE,
                    plot_r_project = FALSE,
                    plot_r_max = FALSE,
                    add = FALSE)

#Example 2
data("simulatedColons")
intrinsic_mean<-
  intrinsic_mean_tube(tubes = simulatedColons,
                    plotting = FALSE)

# Plotting
plot_Elliptical_Tube(tube = intrinsic_mean,
                    plot_frames = FALSE,
                    plot_skeletal_sheet = FALSE,
                    plot_r_project = FALSE,
                    plot_r_max = FALSE,
                    add = FALSE)
```

---

intrinsic\_Transformation\_Elliptical\_Tubes

*Intrinsic Transformation Between Two ETReps*

---

**Description**

Performs the intrinsic transformation from one ETRep to another.

**Usage**

```
intrinsic_Transformation_Elliptical_Tubes(
  tube1,
  tube2,
  type = "sizeAndShapeAnalysis",
  numberOfSteps = 5,
  plotting = TRUE,
```

```

    colorBoundary = "blue"
  )

```

### Arguments

tube1	List containing details of the first ETRep.
tube2	List containing details of the second ETRep.
type	String defining the type of analysis as sizeAndShapeAnalysis or shapeAnalysis
numberOfSteps	Integer, number of transformation steps.
plotting	Logical, enables visualization during transformation (default is TRUE).
colorBoundary	String defining the color of the e-tube

### Value

List containing intermediate ETReps.

### Examples

```

# Load tubes
data("tube_A")
data("tube_B")
numberOfSteps <- 10
transformation_Tubes<-
  intrinsic_Transformation_Elliptical_Tubes(
    tube1 = tube_A,tube2 = tube_B,
    numberOfSteps = numberOfSteps,
    plotting = FALSE)
# Plotting
for (i in 1:length(transformation_Tubes)) {
  plot_Elliptical_Tube(tube = transformation_Tubes[[i]],
    plot_frames = FALSE,plot_skeletal_sheet = FALSE
    ,plot_r_project = FALSE,
    plot_r_max = FALSE,
    add = FALSE)
}

```

---

nonIntrinsic\_Distance\_Between2tubes

*Calculating the non-intrinsic distance between two ETReps*

---

### Description

Calculating the non-intrinsic distance between two ETReps

### Usage

```
nonIntrinsic_Distance_Between2tubes(tube1, tube2)
```

**Arguments**

tube1            List containing ETRep details.  
tube2            List containing ETRep details.

**Value**

Numeric

**Examples**

```
# Load tubes  
data("tube_A")  
data("tube_B")  
intrinsic_Distance_Between2tubes(tube1 = tube_A, tube2 = tube_B)
```

---

nonIntrinsic\_mean\_tube

*Calculate Non-Intrinsic Mean of ETReps*

---

**Description**

Computes the non-intrinsic mean of a set of ETReps.

**Usage**

```
nonIntrinsic_mean_tube(tubes, type = "sizeAndShapeAnalysis", plotting = TRUE)
```

**Arguments**

tubes            List of ETReps.  
type            String, "ShapeAnalysis" or "sizeAndShapeAnalysis" (default is "sizeAndShapeAnalysis").  
plotting        Logical, enables visualization of the mean (default is TRUE).

**Value**

List representing the mean ETRep.

**Examples**

```
#Example 1  
# Load tubes  
data("tube_A")  
data("tube_B")  
nonIntrinsic_mean<-  
  nonIntrinsic_mean_tube(tubes = list(tube_A, tube_B),  
                        plotting = FALSE)
```



```

# Plotting
plot_Elliptical_Tube(tube = nonIntrinsic_mean,
                     plot_frames = FALSE,
                     plot_skeletal_sheet = FALSE,
                     plot_r_project = FALSE,
                     plot_r_max = FALSE,
                     add = FALSE)

#Example 2
data("simulatedColons")
nonIntrinsic_mean<-
  nonIntrinsic_mean_tube(tubes = simulatedColons,
                        plotting = FALSE)

# Plotting
plot_Elliptical_Tube(tube = nonIntrinsic_mean,
                     plot_frames = FALSE,
                     plot_skeletal_sheet = FALSE,
                     plot_r_project = FALSE,
                     plot_r_max = FALSE,
                     add = FALSE)

```

---

nonIntrinsic\_Transformation\_Elliptical\_Tubes

*Non-intrinsic Transformation Between Two ETReps*

---

## Description

Performs the non-intrinsic transformation from one ETRep to another.

## Usage

```

nonIntrinsic_Transformation_Elliptical_Tubes(
  tube1,
  tube2,
  type = "sizeAndShapeAnalysis",
  numberOfSteps = 4,
  plotting = TRUE,
  colorBoundary = "blue",
  add = FALSE
)

```

## Arguments

tube1	List containing details of the first ETRep.
tube2	List containing details of the second ETRep.
type	String defining the type of analysis as sizeAndShapeAnalysis or shapeAnalysis
numberOfSteps	Integer, number of transformation steps.
plotting	Logical, enables visualization during transformation (default is TRUE).

colorBoundary String defining the color of the e-tube  
 add Logical, enables overlay plotting

### Value

List containing intermediate ETReps.

### Examples

```
# Load tubes
data("tube_A")
data("tube_B")
numberOfSteps <- 10
transformation_Tubes<-
  nonIntrinsic_Transformation_Elliptical_Tubes(
    tube1 = tube_A,tube2 = tube_B,
    numberOfSteps = numberOfSteps,
    plotting = FALSE)
# Plotting
for (i in 1:length(transformation_Tubes)) {
  plot_Elliptical_Tube(tube = transformation_Tubes[[i]],
    plot_frames = FALSE,plot_skeletal_sheet = FALSE
    ,plot_r_project = FALSE,
    plot_r_max = FALSE,
    add = FALSE)
}
```

---

plot\_Elliptical\_Tube *Plot an Elliptical Tube (ETRep)*

---

### Description

Plots a given ETRep with options for boundary, material frames, and projection visualization.

### Usage

```
plot_Elliptical_Tube(
  tube,
  plot_boundary = TRUE,
  plot_r_max = FALSE,
  plot_r_project = TRUE,
  plot_frames = TRUE,
  frameScaling = NA,
  plot_spine = TRUE,
  plot_normal_vec = FALSE,
  plot_skeletal_sheet = TRUE,
  decorate = TRUE,
  colSkeletalSheet = "blue",
```

```

    colorBoundary = "blue",
    add = FALSE
  )

```

### Arguments

<code>tube</code>	List containing ETRep details.
<code>plot_boundary</code>	Logical, enables plotting of the boundary (default is TRUE).
<code>plot_r_max</code>	Logical, enables plotting of max projection size (default is FALSE).
<code>plot_r_project</code>	Logical, enables plotting of projection along normals (default is TRUE).
<code>plot_frames</code>	Logical, enables plotting of the material frames (default is TRUE).
<code>frameScaling</code>	Numeric, scale factor for frames.
<code>plot_spine</code>	Logical, enables plotting of the spine.
<code>plot_normal_vec</code>	Logical, enables plotting of the normals.
<code>plot_skeletal_sheet</code>	Logical, enables plotting of the surface skeleton.
<code>decorate</code>	Logical, enables decorate the plot
<code>colSkeletalSheet</code>	String, defining the color of the surface skeleton
<code>colorBoundary</code>	String, defining the color of the e-tube
<code>add</code>	Logical, enables overlay plotting

### Value

Graphical output.

### Examples

```

# Load tube
data("colon3D")
plot_Elliptical_Tube(tube = colon3D,
                    plot_frames = FALSE,
                    add=FALSE)

```

---

simulatedColons

*Data*

---

### Description

Simulated samples of e-tubes, modeled after a reference structure resembling a colon.

### Usage

```
simulatedColons
```

**Format**

Five simulated samples of elliptical tubes, modeled after a reference structure resembling a colon.

**Source**

Generated and stored in the package's 'data/' folder.

---

simulate_etube	<i>Simulate Random Elliptical Tubes (ETReps)</i>
----------------	--

---

**Description**

Generates random samples of ETReps based on a reference tube with added variation.

**Usage**

```
simulate_etube(
  referenceTube,
  numberOfSimulation,
  sd_v = 10^-10,
  sd_psi = 10^-10,
  sd_x = 10^-10,
  sd_a = 10^-10,
  sd_b = 10^-10,
  rangeSdScale = c(1, 2),
  plotting = TRUE
)
```

**Arguments**

referenceTube	List containing ETRep information as the reference.
numberOfSimulation	Integer, number of random samples.
sd_v	Standard deviations for various parameters.
sd_psi	Standard deviations for various parameters.
sd_x	Standard deviations for various parameters.
sd_a	Standard deviations for various parameters.
sd_b	Standard deviations for various parameters.
rangeSdScale	Numeric range for random scaling.
plotting	Logical, enables visualization of samples (default is FALSE).

**Value**

List of random ETReps.

**Examples**

```
# Load tube
data("colon3D")
#Set Parameters
sd_v<-sd_psi<-1e-03
sd_x<-sd_a<-sd_b<-1e-04
numberOfSimulation<-3
random_Tubes<-
  simulate_etube(referenceTube = colon3D,
                 numberOfSimulation = numberOfSimulation,
                 sd_v = sd_v,
                 sd_psi = sd_psi,
                 sd_x = sd_x,
                 sd_a = sd_a,
                 sd_b = sd_b,
                 rangeSdScale = c(1, 2),
                 plotting = FALSE)

# Plotting
rgl::open3d()
for (i in 1:numberOfSimulation) {
  plot_Elliptical_Tube(tube = random_Tubes[[i]],
                      plot_frames = FALSE,
                      plot_skeletal_sheet = FALSE,
                      plot_r_project = FALSE,
                      plot_r_max = FALSE,
                      add = TRUE)
}
```

---

tube\_A

*Data*

---

**Description**

A tube with 204 elliptical cross-sections.

**Usage**

tube\_A

**Format**

A list containing the information of an e-tube with 204 elliptical cross-sections

**Source**

Generated and stored in the package's 'data/' folder.

---

tube\_B

*Data*

---

**Description**

A tube with 204 elliptical cross-sections.

**Usage**

tube\_B

**Format**

A list containing the information of an e-tube with 204 elliptical cross-sections

**Source**

Generated and stored in the package's 'data/' folder.

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